

St William of York Calculation Policy

## Calculation policy, KS1

The following pages show progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children's confidence in their understanding of both written and mental methods.

## **KEY STAGE 1**

Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. They learn how to use an understanding of 10s and 1s to develop their calculation strategies, especially in addition and subtraction.

**Key language:** whole, part, ones, ten, tens, number bond, add, addition, plus, total, altogether, subtract, subtraction, find the difference, take away, minus, less, more, group, share, equal, equals, is equal to, groups, equal groups, times, multiply, multiplied by, divide, share, shared equally, times-table

Year 1 Addition	<b>Counting and adding more</b> Children add one more person or object to a group to find one more.	Counting and adding more Children add one more cube or counter to a group to represent one more.	Counting and adding more Use a number line to understand how to link counting on with finding one more.
			one more 0 1 2 3 4 5 6 7 8 9 10
		One more than 4 is 5.	One more than 6 is 7. 7 is one more than 6.
			Learn to link counting on with adding more than one. 0  1  2  3  4  5  6  7  8  9  10 5 + 3 = 8
	Understanding part-part-whole relationship Sort people and objects into parts and understand the relationship with the whole.	Understanding part-part-whole relationship Children draw to represent the parts and understand the relationship with the whole.	Understanding part-part-whole relationship Use a part-whole model to represent the numbers. 10 6 $46 + 4 = 106 + 4 = 10$
	Knowing and finding number bonds within 10 Break apart a group and put back together to find and form number bonds.	Knowing and finding number bonds within 10 Use five and ten frames to represent key number bonds.	Knowing and finding number bonds within 10 Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero.

<i>3</i> + 4 = 7	5 = 4 + 1	
6 = 2 + 4	10 = 7 + 3	b) $3 1$ 4 + 0 = 4
Understanding teen numbers as a complete 10 and some more Complete a group of 10 objects and count more.	Understanding teen numbers as a complete 10 and some more Use a ten frame to support understanding of a complete 10 for teen numbers.	3 + 1 = 4 Understanding teen numbers as a complete 10 and some more. 1 ten and 3 ones equal 13. 10 + 3 = 13
<ul> <li>13 is 10 and 3 more.</li> <li>Adding by counting on Children use knowledge of counting to 20 to find a total by counting on using people or objects.</li> </ul>	13 is 10 and 3 more. Adding by counting on Children use counters to support and represent their counting on strategy.	Adding by counting on Children use number lines or number tracks to support their counting on strategy.

	<b>Adding the 1s</b> Children use bead strings to recognise how to add the 1s to find the total efficiently. 2 + 3 = 5 12 + 3 = 15	Adding the 1s Children represent calculations using ten frames to add a teen and 1s. 2+3=5 $12+3=15$	7 $7$ $7 + 5 =$ $7 + 5 =$ Adding the 1s $7 + 5 =$ Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently. $3 + 5 = 8$ So, $13 + 5 = 18$
	Bridging the 10 using number bonds Children use a bead string to complete a 10 and understand how this relates to the addition. 	Bridging the 10 using number bonds Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.	Bridging the 10 using number bonds Use a part-whole model and a number line to support the calculation. 4 1 3 9 10 11 12 13 9 + 4 = 13
Year 1 Subtraction	Counting back and taking away Children arrange objects and remove to find how many are left.	<b>Counting back and taking away</b> Children draw and cross out or use counters to represent objects from a problem.	<b>Counting back and taking away</b> Children count back to take away and use a number line or number track to support the method.

1 less than 6 is 5. 6 subtract 1 is 5.	• • • • • • • • • • • • • • • • • • •	9 - 3 = 6
Finding a missing part, given a whole and a part Children separate a whole into parts and understand how one part can be found by subtraction. $\downarrow \qquad \qquad$	Finding a missing part, given a whole and a part Children represent a whole and a part and understand how to find the missing part by subtraction. 5 - 4 = 1	Finding a missing part, given a whole and a part Children use a part-whole model to support the subtraction to find a missing part. 7 - 3 = ? Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model. - = = + = = + = =
Finding the difference Arrange two groups so that the difference between the groups can be worked out.	Finding the difference Represent objects using sketches or counters to support finding the difference.	Finding the difference Children understand 'find the difference' as subtraction. 0 1 2 3 4 5 6 7 8 9 10

Image: Second system       Image: Second system         Image: Second	5 – 4 = 1 The difference between 5 and 4 is 1.	10 – 4 = 6 The difference between 10 and 6 is 4.
Subtraction within 20 Understand when and how to subtract 1s efficiently. Use a bead string to subtract 1s efficiently. 5-3=2 15-3=12	Subtraction within 20 Understand when and how to subtract 1s efficiently. $\bigcirc \bigcirc $	Subtraction within 20 Understand how to use knowledge of bonds within 10 to subtract efficiently. 5 - 3 = 2 15 - 3 = 12
Subtracting 10s and 1s For example: 18 – 12 Subtract 12 by first subtracting the 10, then the remaining 2. First subtract the 10, then take away 2.	Subtracting 10s and 1s         For example: 18 – 12         Use ten frames to represent the efficient method of subtracting 12.         Image: Comparison of the subtract of the	Subtracting 10s and 1s Use a part-whole model to support the calculation. 14 19 - 14 19 - 14 19 - 10 = 9 9 - 4 = 5 So, $19 - 14 = 5$
Subtraction bridging 10 using number bonds For example: 12 – 7 Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.	Subtraction bridging 10 using number bonds Represent the use of bonds using ten frames.	Subtraction bridging 10 using number bonds Use a number line and a part-whole model to support the method. 13 – 5

	7 is 2 and 5, so I take away the 2 and then the 5.	For 13 – 5, I take away 3 to make 10, then take away 2 to make 8.	5 6 7 8 9 10 11 12 13
Year 1 Multiplication	Recognising and making equal groups         Children arrange objects in equal and         unequal groups and understand how to         recognise whether they are equal.         A       B       C         Image: Second Secon	Recognising and making equal groups Children draw and represent equal and unequal groups.	<b>Describe equal groups using words</b> <i>Three equal groups of 4.</i> <i>Four equal groups of 3.</i>
	Finding the total of equal groups by counting in 2s, 5s and 10s There are 5 pens in each pack 510152025303540	Finding the total of equal groups by counting in 2s, 5s and 10s         100 squares and ten frames support counting in 2s, 5s and 10s.         100 squares and ten frames support counting in 2s, 5s and 10s.         100 squares and ten frames support counting in 2s, 5s and 10s.         100 squares and ten frames support counting in 2s, 5s and 10s.         100 squares and ten frames support counting in 2s, 5s and 10s.         100 squares and ten frames support counting in 2s, 5s and 10s.         101 squares and ten frames support counting in 2s, 5s and 10s.         102 squares and ten frames support counting in 2s, 5s and 10s.         101 squares and ten frames support counting in 2s, 5s and 10s.         102 squares and ten frames support counting in 2s, 5s and 10s.         101 squares and ten frames support counting in 2s, 5s and 10s.         11 squares and ten frames support counting in 2s, 5s and 10s.         11 squares and ten frames support counting in 2s, 5s and 10s.         11 squares and ten frames support counting in 2s, 5s and 10s.         11 squares and ten frames support counting in 2s, 5s and 10s.         11 squares and ten frames support counting in 2s, 5s and 10s.         12 squares and ten frames support counting in 2s, 5s and 10s.         13 squares and ten frames support counting in 2s, 5s and 10s.         14 squares and ten frames support counting in 2s, 5s and 10s.	Finding the total of equal groups by counting in 2s, 5s and 10s Use a number line to support repeated addition through counting in 2s, 5s and 10s. 10  10  10  10  10  10  10  10
Year 1 Division	<b>Grouping</b> Learn to make equal groups from a whole and find how many equal groups of a certain size can be made. Sort a whole set people and objects into equal groups.	Grouping Represent a whole and work out how many equal groups.	Grouping Children may relate this to counting back in steps of 2, 5 or 10.

There are 10 children altogether. There are 2 in each group. There are 5 groups.	There are 2 groups.	
Sharing Share a set of objects into equal parts and work out how many are in each part.	Sharing         Sketch or draw to represent sharing into         equal parts. This may be related to         fractions.         Image: Second state of the second state of	<b>Sharing</b> 10 shared into 2 equal groups gives 5 in each group.

	Year 2			
	Concrete	Pictorial	Abstract	
Year 2 Addition				
Understanding 10s and 1s	Group objects into 10s and 1s.	Understand 10s and 1s equipment, and link with visual representations on ten frames.	Represent numbers on a place value grid, using equipment or numerals. Tens Ones 3 2 Tens Ones 4 3	
Adding 10s	Use known bonds and unitising to add 10s. ())) ()) ()) ()) ()) ()) ()) ()) ()) ()	Use known bonds and unitising to add 10s. Use known bonds and unitising to add 10s. H = 0 H = 0	Use known bonds and unitising to add 10s. $\begin{array}{r} 7\\ 4\\ 3\\ 4+3=\end{array}$ $\begin{array}{r} 4+3=7\\ 4\ tens+3\ tens=7\ tens\\ 40+30=70\end{array}$	
Adding a 1-digit number to a 2-digit number not	Add the 1s to find the total. Use known bonds within 10.	Add the 1s.	Add the 1s. Understand the link between counting on and using known number facts. Children	

bridging a 10	41 is 4 tens and 1 one. 41 add 6 ones is 4 tens and 7 ones. This can also be done in a place value grid.	+ + + + + + + + + + + + + + + + + + +	should be encouraged to use known number bonds to improve efficiency and accuracy. 30 3I 32 33 34 35 36 37 38 39 40 This can be represented horizontally or vertically. 34 + 5 = 39 or T O 3 4 4 5 9
Adding a 1-digit number to a 2-digit number bridging 10	Complete a 10 using number bonds. + + + + + + + + + + + + + + + + + + +	Complete a 10 using number bonds.	Complete a 10 using number bonds. 7 $5$ $2$ $+5$ $+2$ $43$ $44$ $45$ $46$ $47$ $48$ $49$ $50$ $51$ $52$ $53$ $7 = 5 + 2$ $45 + 5 + 2 = 52$
Adding a 1-digit number to a 2-digit number using exchange	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.	Exchange 10 ones for 1 ten.

Adding a multiple of 10 to a 2-digit number	Image: constraint of the second se	T O Add the 10s and then recombine. Add the 10s and then recombine. 4dd the 10s and then recombine. $66 is 6 tens and 6 ones.$ $66 + 10 = 76$ A 100 square can support this understanding. $1 \frac{2}{2} \frac{2}{2} \frac{4}{2} \frac{5}{5} \frac{6}{7} \frac{8}{7} \frac{8}{9} \frac{9}{10}$ $\frac{1}{2} \frac{2}{2} \frac{2}{2} \frac{5}{5} \frac{5}{7} \frac{7}{7} \frac{8}{7} \frac{9}{10}$	T = 0 $T = 0$
Adding a multiple of 10 to a 2-digit number using columns	Add the 10s using a place value grid to support.	Add the 10s using a place value grid to support.	Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value.

	T       O         Image: Constraint of the state of the	T       O         Image: Constraint of the system       Image: Constraint of the system         16 is 1 ten and 6 ones.       Image: Constraint of the system         30 is 3 tens.       Image: Constraint of the system         There are 4 tens and 6 ones in total.	$\begin{array}{c c} T & O \\ I & 6 \\ + & 3 & 0 \\ \hline 4 & 6 \end{array}$ $\begin{array}{c} 1 + 3 = 4 \\ 1 \ ten + 3 \ tens = 4 \ tens \\ 16 + 30 = 46 \end{array}$
Adding two 2-digit numbers	Add the 10s and 1s separately. Add the 10s and 1s separately. 5+3=8 There are 8 ones in total. 3+2=5 There are 5 tens in total. 35+23=58	Add the 10s and 1s separately. Use a part-whole model to support. 32 + 11 $11 = 10 + 1$ $32 + 10 = 42$ $42 + 1 = 43$ $32 + 11 = 43$	Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations. $\frac{+10}{17}$ $\frac{+10}{17}$ $\frac{+25}{-10}$ $\frac{17}{17}$ $\frac{+25}{-10}$ 17 + 25
Adding two 2-digit numbers using a place value grid	Add the 1s. Then add the 10s.		Add the 1s. Then add the 10s.

	Tens Ones   Image: state sta		$     \begin{array}{r}       T \\       3 \\       + \\       4 \\       4 \\       6     \end{array}   $ $     \begin{array}{r}       T \\       + \\       4 \\       4 \\       4 \\       4 \\       6   \end{array} $
Adding two 2-digit numbers with exchange	Add the 1s. Exchange 10 ones for a ten. Then add the 10s. Tens Ones 3 6 4 2 9 Tens Ones 9 9 9 9 9 9 9 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		Add the 1s. Exchange 10 ones for a ten. Then add the 10s. $\frac{T}{3} \frac{O}{6} + \frac{2}{9} \frac{Q}{5}$
Year 2 Subtraction			
Subtracting multiples of 10	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.	Use known number bonds and unitising to subtract multiples of 10.

	<ul> <li>Subtract 6 is 2.</li> <li>So, 8 tens subtract 6 tens is 2 tens.</li> </ul>	$ \begin{array}{c c} 100 \\ \hline 30 \\ 10 - 3 = 7 \\ So, 10 tens subtract 3 tens is 7 tens. \end{array} $	7 2 5 20 50 7 tens subtract 5 tens is 2 tens. 70 - 50 = 20
Subtracting a single-digit number	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. This may be done in or out of a place value grid.	Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
Subtracting a single-digit number bridging 10	Bridge 10 by using known bonds.	Bridge 10 by using known bonds.	Bridge 10 by using known bonds. -4 -4 16 17 18 19 20 21 22 23 24 25 26 24 - 6 = ? 24 - 4 - 2 = ?
Subtracting a single-digit number using exchange	Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.	Exchange 1 ten for 10 ones.	Exchange 1 ten for 10 ones.

		T     O       Image: Description of the system     Image: Description of the system       T     O       Image: Description of the system     Image: Description of the system       T     O       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the system       Image: Description of the system     Image: Description of the sys	$ \begin{array}{c} T & O \\ 1 & 2 & 5 \\ - & 7 \\ 8 \\ \hline T & O \\ 1 & 2 & 5 \\ - & 7 \\ 1 & 8 \\ 25 - 7 = 18 \end{array} $
Subtracting a 2-digit number	Subtract by taking away.	Subtract the 10s and the 1s. This can be represented on a 100 square. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Subtract the 10s and the 1s. This can be represented on a number line. -10 $-10$ $-10$ $-10$ $-10$ $-10$ $-10$ $-1023$ $33$ $43$ $53$ $63 6464 - 41 = ?64 - 1 = 6363 - 40 = 2364 - 41 = 23-5$ $-10$ $-1021$ $26$ $36$ $4646 - 20 = 2626 - 5 = 2146 - 25 = 21$
Subtracting a 2-digit number using place value and	Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid.	Subtract the 1s. Then subtract the 10s.	Using column subtraction, subtract the 1s. Then subtract the 10s.

columns	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Tens Ones	T O 4 5 - I 2 3 T O 4 5 - I 2 3 3
Subtracting a 2-digit number with exchange		Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.	Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s. $\frac{T O}{4 5}$ $-2 7$ $\frac{T O}{3 \# 5}$ $-2 7$ $\frac{T O}{3 \# 5}$ $-2 7$ $\frac{T O}{3 \# 5}$ $-2 7$ $\frac{8}{8}$ $\frac{T O}{3 \# 5}$ $-2 7$ $\frac{8}{18}$
Year 2 Multiplication			
Equal groups and repeated	Recognise equal groups and write as repeated addition and as multiplication.	Recognise equal groups using standard objects such as counters and write as	Use a number line and write as repeated addition and as multiplication.

addition		repeated addition and multiplication.	
	3 groups of 5 chairs 15 chairs altogether	3 groups of 5 15 in total	$ \begin{array}{c}                                     $
Using arrays to represent multiplication	Understand the relationship between arrays, multiplication and repeated addition.	Understand the relationship between arrays, multiplication and repeated addition.	Understand the relationship between arrays, multiplication and repeated addition.
and support understanding			
	4 groups of 5	4 groups of 5 5 groups of 5	5 × 5 = 25
Understanding commutativity	Use arrays to visualise commutativity.	Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.	Use arrays to visualise commutativity.
	I can see 6 groups of 3. I can see 3 groups of 6.	This is 2 groups of 6 and also 6 groups of 2.	4 + 4 + 4 + 4 + 4 = 20 5 + 5 + 5 + 5 = 20 4 × 5 = 20 and 5 × 4 = 20
Learning ×2, ×5 and ×10 table facts	Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.	Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.	Understand how the times-tables increase and contain patterns.

		00000000	
		00000000	10 10
	3 groups of 10 10, 20, 30 3 × 10 = 30	$ \begin{array}{c} \bullet $	10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10         10       10       10       10         10       10       10       10       10         10       10       10       10       10         10       10       10       10       10         10       10       10       10       10         10       10       10       10       10
Year 2 Division			$10 10 10 10 10 10 10 10 10 10 10 10$ $5 \times 10 = 50$ $6 \times 10 = 60$
Sharing equally	Start with a whole and share into equal parts, one at a time.	Represent the objects shared into equal parts using a bar model.	Use a bar model to support understanding of the division.

	<ul> <li>12 shared equally between 2.</li></ul>	20 shared into 5 equal parts.	<sup>18</sup>
	They get 6 each. <li>Start to understand how this also relates to grouping. To share equally between 3 people, take a group of 3 and give 1 to each person. Keep going until all the objects have been shared</li> <li>Image: Start to the start of the</li>	There are 4 in each part.	18 ÷ 2 = 9
Grouping equally	Understand how to make equal groups from a whole.	Understand the relationship between grouping and the division statements.	Understand how to relate division by grouping to repeated subtraction.

		$12 \div 3 = 4$ $12 \div 4 = 3$ $12 \div 6 = 2$ $12 \div 2 = 6$	There are 4 groups of 3. $12 \div 3 = 4$ There are 4 groups.
Using known times-tables to solve divisions	Understand the relationship between multiplication facts and division.	Link equal grouping with repeated subtraction and known times-table facts to support division. 40  divided by 4 is 10. Use a bar model to support understanding of the link between times-table knowledge and division.	Relate times-table knowledge directly to division. $1 \times 10 = 10$ $2 \times 10 = 20$ $3 \times 10 = 30$ $4 \times 10 = 40$ $5 \times 10 = 50$ $6 \times 10 = 60$ $7 \times 10 = 70$ $8 \times 10 = 80$ <i>I</i> used the 10 times-table to help me. $3 \times 10 = 30$ . <i>I</i> know that 3 groups of 10 makes 30, so 1 know that 30 divided by 10 is 3. $3 \times 10 = 30$ so $30 \div 10 = 3$